
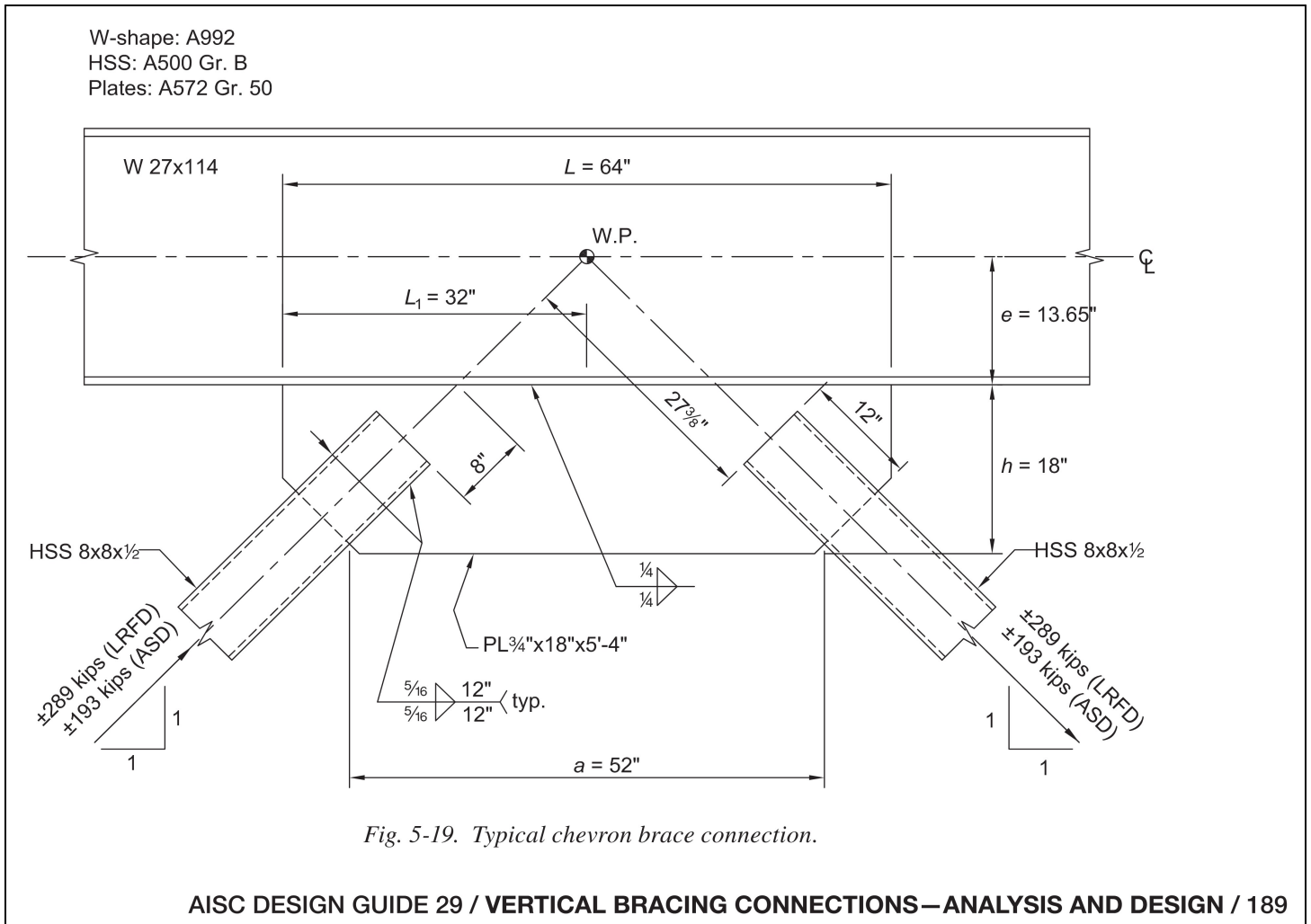


ORIGIN := 1

Reference to AISC 14th Edition shapes database:

T1 :=  Row(shape) := for i ∈ 1..rows(T1) - 1
 $R \leftarrow i$ if $(T1^{(2)})_i = \text{shape}$
 R

Solve Example 5.9 Chevron Brace Connection



Loads

LRFD Brace axial force
note : similar in both braces

$$P_u := 289 \text{ kip}$$

Material Properties

Beams steel grade A992

$$F_{y_{\text{beam}}} := 50 \cdot \text{ksi}$$

$$F_{u_{\text{beam}}} := 65 \cdot \text{ksi}$$

Brace steel grade A500 GrB

$$F_{y_{\text{brace}}} := 46 \cdot \text{ksi}$$

$$F_{u_{\text{brace}}} := 58 \cdot \text{ksi}$$

Plate steel grade A572 Gr. 50

$$F_{y_{\text{PL}}} := 50 \text{ ksi}$$

$$F_{u_{\text{PL}}} := 65 \text{ ksi}$$

Modulus of Elasticity

$$E := 29000 \text{ ksi}$$

weld strength

$$F_{EXX} := 70 \text{ ksi}$$

$$C_1 := 1.0$$

Member Properties**Beam Properties**

Beam section

$$\text{Beam} := \text{"W27X114"}$$

depth of beam

$$d_{\text{beam}} := T1(\text{Row}(\text{Beam}), 7) \cdot \text{in} = 27.3 \cdot \text{in}$$

width of flange

$$b_{f_{\text{beam}}} := T1(\text{Row}(\text{Beam}), 12) \cdot \text{in} = 10.1 \cdot \text{in}$$

thickness of flange

$$t_{f_{\text{beam}}} := T1(\text{Row}(\text{Beam}), 20) \cdot \text{in} = 0.93 \cdot \text{in}$$

thickness of web

$$t_{w_{\text{beam}}} := T1(\text{Row}(\text{Beam}), 17) \cdot \text{in} = 0.57 \cdot \text{in}$$

design weld depth

$$k_{\text{des}_{\text{brace}}} := T1(\text{Row}(\text{Beam}), 25) \cdot \text{in} = 1.53 \cdot \text{in}$$

Brace Properties

Brace section

$$\text{Brace} := \text{"HSS8X8X.500"}$$

cross sectional area

$$A_{g_{\text{brace}}} := T1(\text{Row}(\text{Brace}), 6) \cdot \text{in}^2 = 13.5 \cdot \text{in}^2$$

radius of gyration

$$r_{\text{brace}} := T1(\text{Row}(\text{Brace}), 42) \cdot \text{in} = 3 \cdot \text{in}$$

this is the r.x value
(sim to r.y for square shapes)

depth to end of weld

$$t_{\text{des}_{\text{brace}}} := T1(\text{Row}(\text{Brace}), 24) \cdot \text{in} = 0.465 \cdot \text{in}$$

$$B := T1(\text{Row}(\text{Brace}), 9) \cdot \text{in} = 8 \cdot \text{in}$$

$$H := T1(\text{Row}(\text{Brace}), 14) \cdot \text{in} = 8 \cdot \text{in}$$

slope of brace

$$\text{slope} := \text{atan}\left(\frac{12}{12}\right) = 45 \cdot \text{deg}$$

Plate Properties

thickness $t_{PL} := 0.75\text{in}$
 length $L := 64\text{in}$
 height $h := 18\text{in}$
 cut length $a := 52\text{in}$

distance brace to W.P. $e_{WP} := 27.375\text{in}$
 eccentricity of brace CL to W.P. $e := 13.65\text{in}$
 end of PL to W.P. length (centered) $L_1 := 32\text{in}$
 $L_2 := L_1$

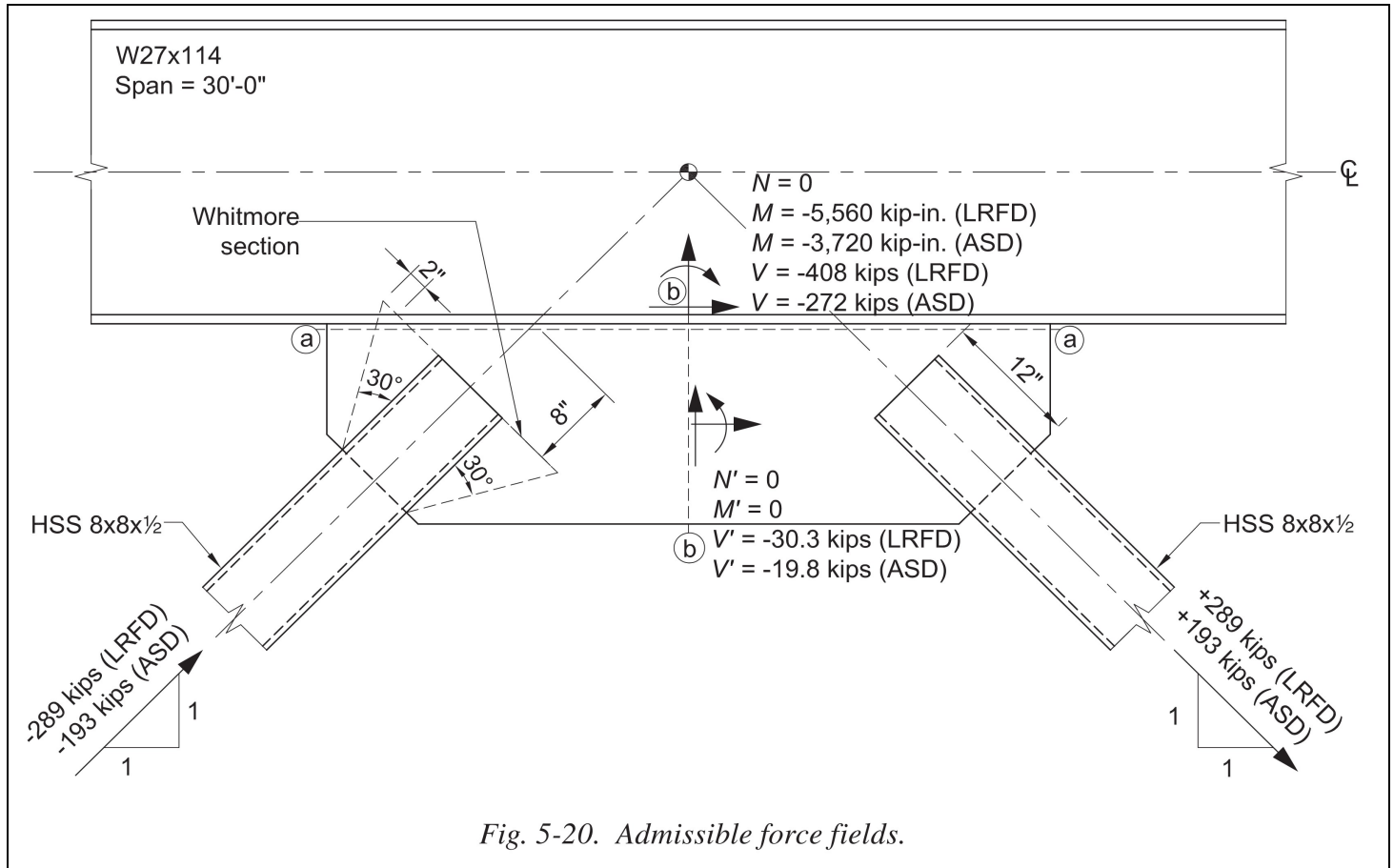


Fig. 5-20. Admissible force fields.

subscript "1" denotes Brace 1, on the left side of Figure 5-19, and the subscript "2" denotes Brace 2 on the right side

$$\Delta := \frac{L_1 - L_2}{2} = \frac{32\text{in} - 32\text{in}}{2} = 0\text{in}$$

$$P_{u1} := -289\text{kip}$$

$$P_{u2} := 289\text{kip}$$

$$H_{u1} := P_{u1} \cdot \cos(\text{slope}) = -204.35 \cdot \text{kip}$$

$$H_{u2} := P_{u2} \cdot \cos(\text{slope}) = 204.4 \cdot \text{kip}$$

$$V_{u1} := P_{u1} \cdot \sin(\text{slope}) = -204.4 \cdot \text{kip}$$

$$V_{u2} := P_{u2} \cdot \sin(\text{slope}) = 204.4 \cdot \text{kip}$$

$$M_{u1} := H_{u1} \cdot e + V_{u1} \cdot \Delta = -2789.4 \cdot \text{kip} \cdot \text{in}$$

$$M_{u2} := H_{u2} \cdot e + V_{u2} \cdot \Delta = 2789.4 \cdot \text{kip} \cdot \text{in}$$

$$M'_{u1} := \frac{1}{8} \cdot V_{u1} \cdot L - \frac{1}{4} \cdot H_{u1} \cdot h - \frac{1}{2} \cdot M_{u1} = 679 \cdot \text{kip} \cdot \text{in}$$

$$M'_{u2} := \frac{1}{8} \cdot V_{u2} \cdot L - \frac{1}{4} \cdot H_{u2} \cdot h - \frac{1}{2} \cdot M_{u2} = -679 \cdot \text{kip} \cdot \text{in}$$

Axial	$N_u := V_{u1} + V_{u2} = 0 \cdot \text{kip}$	recall
Shear	$V_u := H_{u1} - H_{u2} = -408.7 \cdot \text{kip}$	$V_{u1} = -204.4 \text{ kip}$
Moment	$M_u := M_{u1} - M_{u2} = -5578.9 \cdot \text{kip} \cdot \text{in}$	$V_{u2} = 204.4 \text{ kip}$
Axial	$N'_u := \frac{1}{2} \cdot (H_{u1} + H_{u2}) = 0 \cdot \text{kip}$	$H_{u1} = -204.4 \text{ kip}$
Shear	$V'_u := \frac{1}{2} \cdot (V_{u1} - V_{u2}) - \frac{2M_u}{L} = -30 \cdot \text{kip}$	$H_{u2} = 204.4 \text{ kip}$
Moment	$M'_u := M'_{u1} + M'_{u2} = 0 \cdot \text{kip} \cdot \text{in}$	$L = 64 \text{ in}$
		$M'_{u1} = 679.5 \text{ in} \cdot \text{kip}$
		$M'_{u2} = -679.5 \text{ in} \cdot \text{kip}$

Check tension yielding on the brace (J4.1a)

reduction factor	$\phi := 0.90$	recall
tension yielding	$\phi R_n := \phi \cdot F_y \cdot A_{g_{brace}} = 558.9 \cdot \text{kip}$	$F_{y_{brace}} = 46 \cdot \text{ksi}$
	if($P_u < \phi R_n$, "OK", "NOT OK") = "OK"	$A_{g_{brace}} = 13.5 \text{ in}^2$
		$P_u = 289 \text{ kip}$

shear rupture in the brace wall (J4.2b)

reduction factor	$\phi := 0.75$	recall
calculated weld length (4 lengths of weld)	$P_u \leq \phi \cdot 0.6 \cdot F_u \cdot A_{nv} = \phi \cdot 0.6 \cdot F_u \cdot t_{des_{brace}} \cdot (4) \cdot l_{weld}$	$P_u = 289 \text{ kip}$
	$l_{weld} := \frac{P_u}{0.6 \cdot [\phi \cdot F_{u_{brace}} \cdot t_{des_{brace}} \cdot (4)]} = 6 \text{ in}$	$F_{u_{brace}} = 58 \cdot \text{ksi}$
		$t_{des_{brace}} = 0.5 \text{ in}$

check weld strength (EQ: 8-1)

reduction factor	$\phi := 0.75$	recall
try weld size 5/16 inch	$w_{weld} := 5 \text{ in}$ 16 th of an inch	
weld strength	$P_u \leq \phi \cdot R_n = \phi \cdot 0.60 \cdot F_{EXX} \cdot \left(\frac{1}{\sqrt{2}}\right) \cdot w_{weld} \cdot (4) \cdot l_{weld}$	$P_u = 289 \text{ kip}$
minimum weld length	$l_{weld} \geq \frac{P_u}{\phi \cdot 0.60 \cdot F_{EXX} \cdot \left(\frac{1}{\sqrt{2}}\right) \cdot w_{weld} \cdot (4)}$	$F_{EXX} = 70 \text{ ksi}$
	$l_{weld} := \frac{P_u}{\phi \cdot 0.60 \cdot F_{EXX} \cdot \left(\frac{1}{\sqrt{2}}\right) \cdot \frac{w_{weld}}{16} \cdot (4)} = 10.4 \text{ in}$	

check weld strength (EQ: 8-2)

weld strength

$$\Phi \cdot P_n = 1.392D \cdot l_{\text{weld}} \cdot (4)$$

recall

minimum weld length

$$l_{\text{weld}} := \frac{P_u}{1.392 \text{ksi} \cdot w_{\text{weld}} \cdot (4)} = 10.4 \text{ in}$$

$$P_u = 289 \text{ kip}$$

$$w_{\text{weld}} = 5 \text{ in}$$

use $l_{\text{weld}} = 12''$

$$l_{\text{weld}} := 12 \text{ in}$$

Check tensile rupture on the brace (J4.1b)

slot width

$$d_{\text{slot}} := t_{\text{PL}} + \frac{2}{16} \text{ in} = 0.9 \text{ in}$$

recall

$$t_{\text{PL}} = 0.75 \text{ in}$$

Net area

$$A_{\text{nbrace}} := A_{\text{gbrace}} - 2 \cdot t_{\text{desbrace}} \cdot d_{\text{slot}} = 12.69 \text{ in}^2$$

$$A_{\text{gbrace}} = 13.5 \text{ in}^2$$

$$t_{\text{desbrace}} = 0.465 \text{ in}$$

eccentricity of connection

$$x_{\text{bar}} := \frac{B^2 + 2 \cdot B \cdot H}{4(B + H)} = 3 \text{ in}$$

$$B = 8 \text{ in}$$

$$H = 8 \text{ in}$$

Table D3.1, Case 6

shear lag factor

$$U := 1 - \left(\frac{x_{\text{bar}}}{l_{\text{weld}}} \right) = 0.75$$

$$l_{\text{weld}} = 12 \text{ in}$$

Table D3.1, Case 6

$$F_{\text{ubrace}} = 58 \text{ ksi}$$

$$P_u = 289 \text{ kip}$$

effective net area

$$A_{\text{ebrace}} := A_{\text{nbrace}} \cdot U = 9.51 \text{ in}^2$$

reduction factor

$$\Phi := 0.75$$

tensile rupture strength

$$\Phi R_n := \Phi \cdot F_{\text{ubrace}} \cdot A_{\text{ebrace}} = 413.9 \cdot \text{kip}$$

$$\text{if}(P_u < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

Check block shear rupture on the gusset plate (J4.3)

Block shear strength

$$R_n = 0.60F_u \cdot A_{\text{nv}} + U_{\text{bs}} \cdot F_u \cdot A_{\text{nt}} \leq 0.60F_y \cdot A_{\text{gv}} + U_{\text{bs}} \cdot F_u \cdot A_{\text{nt}}$$

recall

$$t_{\text{PL}} = 0.75 \text{ in}$$

gross shear area

$$A_{\text{gvPL}} := 2 \cdot t_{\text{PL}} \cdot l_{\text{weld}} = 18 \text{ in}^2$$

$$l_{\text{weld}} = 12 \text{ in}$$

net shear area

$$A_{\text{nvPL}} := A_{\text{gvPL}} = 18 \text{ in}^2$$

$$F_{\text{yPL}} = 50 \text{ ksi}$$

$$F_{\text{uPL}} = 65 \text{ ksi}$$

$$0.60 \cdot F_{\text{yPL}} \cdot A_{\text{gvPL}} = 540 \cdot \text{kip}$$

$$B = 8 \text{ in}$$

$$0.60 \cdot F_{\text{uPL}} \cdot A_{\text{nvPL}} = 702 \cdot \text{kip}$$

$$P_u = 289 \text{ kip}$$

$$U_{\text{bs}} := 1$$

gross tensile area

$$A_{\text{gtPL}} := t_{\text{PL}} \cdot B = 6 \text{ in}^2$$

net tensile area

$$A_{\text{ntPL}} := A_{\text{gtPL}} = 6 \text{ in}^2$$

$$U_{bs} \cdot F_{uPL} \cdot A_{ntPL} = 390 \cdot \text{kip}$$

reduction factor

$$\phi := 0.75$$

Block shear strength

$$\phi R_n := \phi \cdot (\min(0.60 \cdot F_{yPL} \cdot A_{gvPL}, 0.60 \cdot F_{uPL} \cdot A_{nvPL}) + U_{bs} \cdot F_{uPL} \cdot A_{ntPL}) = 697.5 \cdot \text{kip}$$

$$\text{if}(P_u < \phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

Check the gusset plate for tensile yielding on the Whitmore section (J4.1a)

recall

width of Whitmore section (pg: 9-3)
see sketch above

$$l_w := B + 2 \cdot l_{\text{weld}} \cdot \tan(30\text{deg}) = 21.9 \text{ in}$$

$$B = 8 \text{ in}$$

$$l_{\text{weld}} = 12 \text{ in}$$

gross tensile area

$$A_w := (l_w - 2\text{in}) \cdot t_{PL} + 2\text{in} \cdot (t_{w\text{beam}}) = 16 \text{ in}^2$$

$$t_{PL} = 0.75 \text{ in}$$

reduction factor

$$\phi := 0.90$$

$$t_{w\text{beam}} = 0.57 \text{ in}$$

tensile yielding strength

$$\phi R_n := \phi \cdot F_{yPL} \cdot A_w = 721.5 \cdot \text{kip}$$

$$P_u = 289 \text{ kip}$$

$$\text{if}(P_u < \phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

Check the gusset plate for buckling on the Whitmore section

recall

effective length factor

$$K_{PL} := 0.65$$

$$B = 8 \text{ in}$$

length of plate to buckle

$$L_{PL} := 8 \text{ in}$$

$$t_{PL} = 0.8 \text{ in}$$

radius of gyration

$$r_{PL} := \sqrt{\frac{L_{PL} \cdot t_{PL}^3}{12 \cdot t_{PL} \cdot L_{PL}}} = 0.217 \text{ in}$$

$$\frac{K \cdot L}{r}$$

$$\frac{K_{PL} \cdot L_{PL}}{r_{PL}} = 24 < 25$$

Gusset-to-Beam Connection

Check the gusset plate for tensile yielding and shear yielding along the beam flange (J4.1a & J4.2a)

recall

gross area

$$A_{g_{PL}} := t_{PL} \cdot L = 48 \text{ in}^2$$

$$t_{PL} = 0.75 \text{ in}$$

Shear yielding stress

$$f_{uv} := \frac{|V_u|}{A_{g_{PL}}} = 8.5 \cdot \text{ksi}$$

$$L = 64 \text{ in}$$

$$V_u = -408.7 \cdot \text{kip}$$

reduction factor

$$\Phi := 1.00$$

$$N_u = 0 \cdot \text{kip}$$

$$\Phi R_n := \Phi \cdot 0.60 \cdot F_{y_{PL}} = 30 \text{ ksi}$$

$$M_u = -5578.9 \cdot \text{kip} \cdot \text{in}$$

$$\text{if}(f_{uv} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

$$F_{y_{PL}} = 50 \text{ ksi}$$

Tensile yielding stress
(due to tension)

$$f_{ua} := \frac{N_u}{A_{g_{PL}}} = 0 \cdot \text{ksi}$$

plastic section modulus

$$Z_{PL} := \frac{t_{PL} \cdot L^2}{4} = 768 \text{ in}^3$$

Tensile yielding stress
(due to moment)

$$f_{ub} := \frac{|M_u|}{Z_{PL}} = 7.3 \cdot \text{ksi}$$

Total tensile yielding stress

$$f_{un} := f_{uv} + f_{ub} = 15.8 \cdot \text{ksi}$$

reduction factor

$$\Phi := 0.90$$

$$\Phi R_n := \Phi \cdot F_{y_{PL}} = 45 \text{ ksi}$$

$$\text{if}(f_{un} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

Design weld at gusset-to-beam flange connection (EQ: 8-13)

recall

effective eccentricity of
the shear force

$$e_{\text{effective}} := \frac{M_u}{V_u} = 13.65 \text{ in}$$

$$M_u = -5578.9 \text{ in} \cdot \text{kip}$$

$$V_u = -408.7 \text{ kip}$$

value in table 8-4

$$a_{\text{weld}} := \frac{e_{\text{effective}}}{L} = 0.213$$

$$L = 64 \text{ in}$$

$$C_1 = 1$$

Table 8-4

$$C := 3.458$$

additional ductility (pg: 13-11)

$$\text{ductility} := 1.25$$

reduction factor

$$\Phi := 0.75$$

weld strength

$$V_u < \frac{\Phi R_n}{\text{ductility}} = \frac{(\Phi \cdot C \cdot C_1 \cdot D \cdot L)}{\text{ductility}}$$

$$D_{\text{min}} > \frac{V_u \cdot \text{ductility}}{(\Phi \cdot C \cdot C_1 \cdot L)}$$

minimum weld size

$$D_{\text{min}} := \frac{(|V_u| \div \text{kip}) \cdot \text{ductility}}{\Phi \cdot C \cdot C_1 \cdot (L \div \text{in})} = 3.1$$

use D = 4 / 16th

$$D_{\text{weld}} := 4 \text{ in} \quad 16 \text{ th of an inch}$$

alternative method to determine the required weld size (DG29 Appendix B), (EQ: 8-2 & pg: 8-9)

maximum equivalent normal force	$N_{\max} := N_u + \left \frac{2 \cdot M_u}{L \div 2} \right = 348.7 \cdot \text{kip}$	recall $M_u = -5578.9 \text{ in} \cdot \text{kip}$
minimum equivalent normal force	$N_{\min} := \left N_u - \left \frac{4M_u}{L} \right \right = 348.7 \cdot \text{kip}$	$V_u = -408.7 \text{ kip}$
peak weld resultant force	$R_{\text{peak}} := \sqrt{V_u^2 + N_{\max}^2} = 537.2 \cdot \text{kip}$	$N_u = 0 \text{ kip}$
average weld resultant force	$R_{\text{avg}} := \sqrt{V_u^2 + \left(\frac{N_{\max} + N_{\min}}{2} \right)^2} = 537.2 \cdot \text{kip}$	$L = 64 \text{ in}$
angle of weld loading	$\theta := \text{atan} \left(\frac{N_{\max}}{ V_u } \right) = 40.5 \cdot \text{deg}$	$D_{\min} = 3.1$
weld strength	$R_{\text{avg}} < \frac{\Phi R_n}{\text{ductility}} = \frac{\Phi \cdot 1.392 \cdot (1 + 0.5 \cdot \sin(\theta)^{1.5}) \cdot D \cdot L \cdot (2)}{\text{ductility}}$	$1 + 0.5 \cdot \sin(\theta)^{1.5} = 1.26$
minimum weld size	$D_{\text{min.2}} := \frac{\text{ductility} \cdot (R_{\text{avg}} \div \text{kip})}{1.392 \cdot (1 + 0.5 \cdot \sin(\theta)^{1.5}) \cdot (2) \cdot (L \div \text{in})} = 2.99$	% strength increase
% difference in calculated weld size	$\frac{D_{\min} - D_{\text{min.2}}}{D_{\min}} = 2.93 \cdot \%$	

Check gusset internal strength

Check the gusset plate for shear yielding (J4.2a)

$$\begin{aligned} \Phi &:= 1.00 \\ \Phi R_n &:= \Phi \cdot 0.60 \cdot F_{y_{PL}} \cdot A_{g_{V_{PL}}} = 540 \cdot \text{kip} \\ \text{if}(V'_u < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) &= \text{"OK"} \end{aligned}$$

recall

$$V'_u = -30.01 \cdot \text{kip}$$

$$A_{g_{V_{PL}}} = 18 \text{ in}^2$$

$$F_{y_{PL}} = 50 \text{ ksi}$$

Check gusset stresses on Section b-b for a hypothetical load case (P.1 = P.2= compression)

recall

$$M_{u1_hypothetical} := H_{u1} \cdot e = -2789.4 \cdot \text{kip} \cdot \text{in}$$

$$N'_u = 0 \cdot \text{kip}$$

$$M_{u2_hypothetical} := M_{u1_hypothetical} = -2789.4 \cdot \text{kip} \cdot \text{in}$$

$$M'_u = 0 \cdot \text{kip} \cdot \text{in}$$

$$M'_{u1_hypothetical} := \left(\frac{1}{8} \cdot H_{u1} \cdot L - \frac{1}{4} \cdot V_{u1} \cdot h \right) - \frac{1}{2} \cdot M_{u1_hypothetical}$$

$$M_{u1} = -2789.4 \cdot \text{kip} \cdot \text{in}$$

$$H_{u1} = -204.4 \text{ kip}$$

$$M'_{u1_hypothetical} = 679.5 \text{ in} \cdot \text{kip}$$

$$e = 13.7 \text{ in}$$

$$L = 64 \text{ in}$$

$$M'_{u2_hypothetical} := M'_{u1_hypothetical} = 679.5 \cdot \text{kip} \cdot \text{in}$$

$$V_{u1} = -204.4 \text{ kip}$$

$$N_{u_hypothetical} := H_{u1} + V_{u1} = -408.7 \cdot \text{kip}$$

$$h = 18 \text{ in}$$

$$V_{u_hypothetical} := H_{u1} - V_{u1} = -0 \cdot \text{kip}$$

$$a = 52 \text{ in}$$

$$M_{u_hypothetical} := M_{u1_hypothetical} - M_{u2_hypothetical} = 0 \cdot \text{kip} \cdot \text{in}$$

$$t_{PL} = 0.75 \text{ in}$$

$$F_{yPL} = 50 \text{ ksi}$$

$$N'_{_hypothetical} := \frac{1}{2} \cdot (H_{u1} + V_{u1}) = -204.4 \cdot \text{kip}$$

$$V'_{_hypothetical} := \frac{1}{2} \cdot (H_{u1} - V_{u1}) + \frac{2 \text{ in}}{L} \cdot (V_{u_hypothetical}) = -0 \cdot \text{kip}$$

$$M'_{hypothetical} := M'_{u1_hypothetical} + M'_{u2_hypothetical} = 1359 \cdot \text{kip} \cdot \text{in}$$

worst case equivalent normal
force (compression)
DG 29 Appendix B

$$N_{ue_hypothetical} := |N'_{_hypothetical}| + \frac{M'_{hypothetical}}{h \div 2} \cdot (2) = 506.3 \cdot \text{kip}$$

DG 29 Appendix C.4

$$b := h = 18 \text{ in}$$

$$\lambda := \frac{(b \div t_{PL}) \cdot \sqrt{F_{yPL} \div \text{ksi}}}{5 \cdot \sqrt{475 + \frac{1120}{(a \div b)^2}}} = 1.4$$

$$Q := 1.34 - 0.486 \cdot \lambda = 0.7$$

$$\Phi := 0.9$$

critical buckling stress
DG 29 EQ:C-6

$$\Phi F_{cr} := \Phi \cdot Q \cdot F_{yPL} = 30.2 \cdot \text{ksi}$$

actual (worst case)
compressive stress

$$f_{ua_theoretical} := \frac{N_{ue_hypothetical}}{t_{PL} \cdot h} = 37.5 \cdot \text{ksi}$$

$$\text{if}(f_{ua_theoretical} < \Phi F_{cr}, \text{"OK"}, \text{"NOT OK"}) = \text{"NOT OK"}$$

using 7/8" plate

$$t_{PL} := \frac{7}{8} \text{ in}$$

$$\lambda := \frac{(b \div t_{PL}) \cdot \sqrt{F_{yPL} \div \text{ksi}}}{5 \cdot \sqrt{475 + \frac{1120}{(a \div b)^2}}} = 1.2$$

$$Q := 1.34 - 0.486 \cdot \lambda = 0.8$$

critical buckling stress
DG 29 EQ:C-6

$$\Phi F_{cr} := \Phi \cdot Q \cdot F_{yPL} = 34.5 \cdot \text{ksi}$$

actual (worst case)
compressive stress

$$f_{ua_theoretical} := \frac{N_{ue_hypothetical}}{t_{PL} \cdot h} = 32.1 \cdot \text{ksi}$$

$$\text{if}(f_{ua_theoretical} < \Phi F_{cr}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

plate thickness

$$t_{PL} := \frac{3}{4} \text{ in}$$

$$b := 13.6 \text{ in}$$

see Tamboli (2010)

$$f_u := 29.9 \text{ ksi}$$

$$\lambda := \frac{(b \div t_{PL}) \cdot \sqrt{F_{yPL} \div \text{ksi}}}{5 \cdot \sqrt{475 + \frac{1120}{(a \div b)^2}}} = 1.1$$

$$Q := 1.34 - 0.486 \cdot \lambda = 0.8$$

critical buckling stress
DG 29 EQ:C-6

$$\Phi F_{cr} := \Phi \cdot Q \cdot F_{yPL} = 36.4 \cdot \text{ksi}$$

$$\text{if}(f_u < \Phi F_{cr}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

Check the gusset plate for buckling on the Whitmore section

recall

effective length factor (conservative)

$$K_{buckle} := 1.2$$

$$L_{PL} = 8 \text{ in}$$

length of buckling member

$$L_{buckle} := \frac{L_{PL}}{\sqrt{2}} = 5.66 \text{ in}$$

$$r_{PL} = 0.217 \text{ in}$$

$$A_w = 16.03 \text{ in}^2$$

$$P_u = 289 \text{ kip}$$

$$\frac{K \cdot L}{r}$$

$$\frac{K_{buckle} \cdot L_{buckle}}{r_{PL}} = 31.4 > 25$$

Available critical stress (Table 4-22)

$$\Phi F_{cr} := 41.86 \text{ ksi}$$

Compressive strength (E.3)

$$\Phi P_n := \Phi F_{cr} \cdot A_w = 671.1 \cdot \text{kip}$$

$$\text{if}(P_u < \Phi P_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

Check the gusset plate for sidesway buckling

Compressive strength (E.3)

$$\Phi P_n := \Phi F_{cr} \cdot t_{PL} \cdot L = 2009.3 \cdot \text{kip}$$

$$\text{if}(|N_{u_hypothetical}| < \Phi P_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

recall

$$\Phi F_{cr} = 41.9 \text{ ksi}$$

$$t_{PL} = 0.75 \text{ in}$$

$$L = 64 \text{ in}$$

$$|N_{u_hypothetical}| = 408.7 \cdot \text{kip}$$

check the beam for web local yielding and local cripplingCheck beam web local yielding (J10.2)

length of bearing

strength reduction factor

$$\Phi := 1.0$$

web local yielding strength

$$\Phi R_n := \Phi \cdot F_{ybeam} \cdot t_{wbeam} \cdot (5k_{desbrace} + L) = 2042 \cdot \text{kip}$$

$$\text{if}(N_{max} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

recall

$$N_{max} = 348.7 \cdot \text{kip}$$

$$k_{desbrace} = 1.53 \text{ in}$$

$$t_{wbeam} = 0.57 \text{ in}$$

$$F_{ybeam} = 50 \text{ ksi}$$

$$L = 64 \text{ in}$$

Check beam web shear yielding (J4.2a)

strength reduction factor

$$\Phi := 1.0$$

$$\Phi R_n = \Phi \cdot 0.60 \cdot F_{ybeam} \cdot A_{gvbeam}$$

shear yielding strength

$$\Phi R_n := \Phi \cdot 0.60 \cdot F_{ybeam} \cdot t_{wbeam} \cdot L = 1094.4 \cdot \text{kip}$$

$$\text{if}(|N_{u_hypothetical}| < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

recall

$$F_{ybeam} = 50 \text{ ksi}$$

$$t_{wbeam} = 0.57 \text{ in}$$

$$L = 64 \text{ in}$$

$$N_{u_hypothetical} = -408.7 \cdot \text{kip}$$

recall

$$E = 29000 \text{ ksi}$$

$$t_{fbeam} = 0.93 \text{ in}$$

$$d_{beam} = 27.3 \text{ in}$$

Check beam web local crippling (J10.3)

strength reduction factor

$$\Phi := 0.75$$

web local crippling strength

$$\Phi R_n := \Phi \cdot 0.80 \cdot t_{wbeam}^2 \cdot \left[1 + 3 \cdot \left(\frac{L}{d_{beam}} \right) \cdot \left(\frac{t_{wbeam}}{t_{fbeam}} \right)^{1.5} \right] \cdot \sqrt{\frac{E \cdot F_{ybeam} \cdot t_{fbeam}}{t_{wbeam}}} = 1311.7 \cdot \text{kip}$$

$$\text{if}(N_{max} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

Check transverse section web yielding (G2.1)

Area of beam web

$$V_u := H_{u2} + V'_u = 174.3 \cdot \text{kip}$$

$$A_{wbeam} := t_{wbeam} \cdot d_{beam} = 15.6 \text{ in}^2$$

strength reduction factor

$$\Phi := 1.0 \quad C_v := 1.0$$

shear yielding strength

$$\Phi V_n := \Phi \cdot 0.6 \cdot F_{ybeam} \cdot A_{wbeam} \cdot C_v = 466.8 \cdot \text{kip}$$

$$\text{if}(V_u < \Phi V_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

recall

$$H_{u2} = 204.4 \cdot \text{kip}$$

$$V'_u = -30 \cdot \text{kip}$$

$$F_{ybeam} = 50 \text{ ksi}$$

$$t_{wbeam} = 0.57 \text{ in}$$

$$d_{beam} = 27.3 \text{ in}$$